

Graph Neural Network Introduction

Table-ronde IBISC du 13/11/2020

Graph definition

- A graph is defined as $\mathcal{G}(\mathcal{V}, \mathcal{E})$ where \mathcal{V} is a set of connected n vertices/nodes and \mathcal{E} is a set of m edges.
- An attribute, a d -dimensional feature vector, can characterize each vertex :
 $X(x_1, \dots, x_n)$.
- $\mathcal{N}(v)$ refers to the neighborhood of the node v .
- $A \in \mathbb{R}^{|\mathcal{V}| \times |\mathcal{V}|}$ defines the adjacency matrix.

Objectives of a Graph Neural Network (GNN)

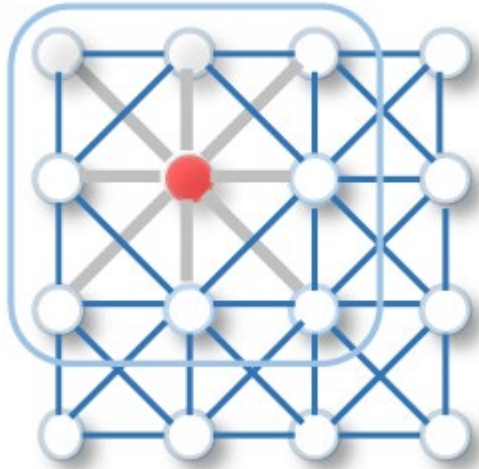
Deep learning approach for **graph-based data** for supervised as well as unsupervised tasks.

The aims of these methods is to:

- predict **final states** of the graph components at global or local scale;
- build a **high-level representation** of any node recursively from the representation vectors of its **neighborhood**.

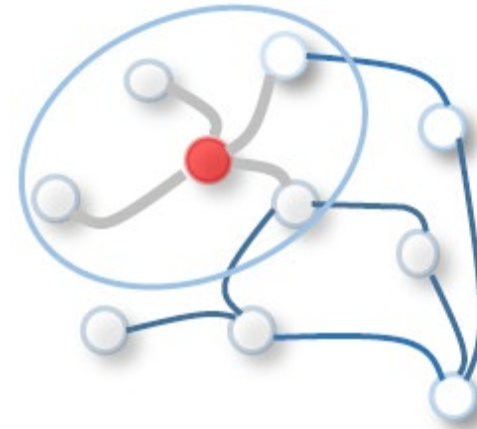
Graph Convolution Network (GCN)

- **Spatial convolution:**



2D Convolution with a CNN

vs

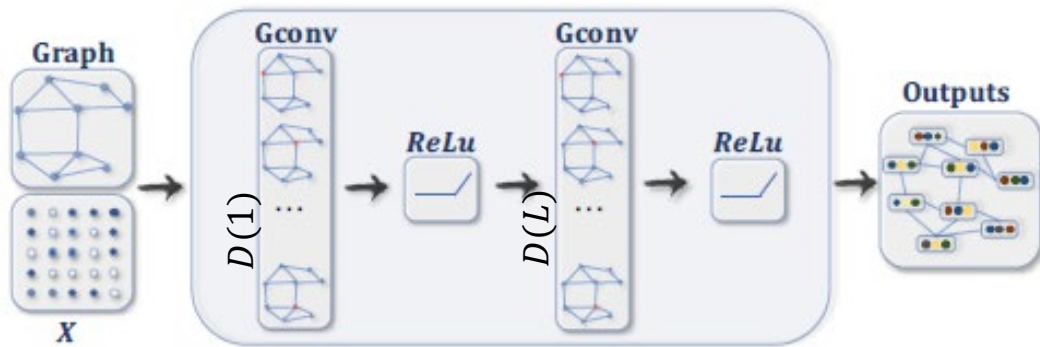


Graph Convolution

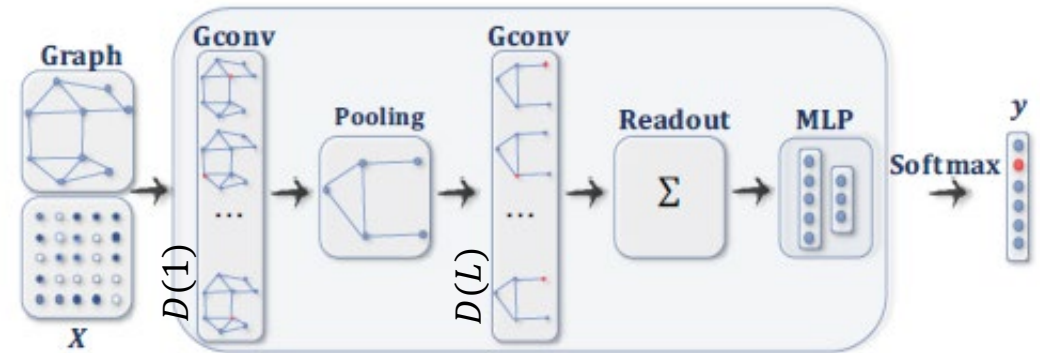
- Can deal with graphs with **different structure**.
- **Key works:** GCN (Kipf et al. (2017)), GraphSAGE (Hamilton et al. (2017)), GIN (Xu et al. (2019)), GAT (Veličković et al. (2018)).

Types of classification

- **3 types:** edge, **node**, graph.



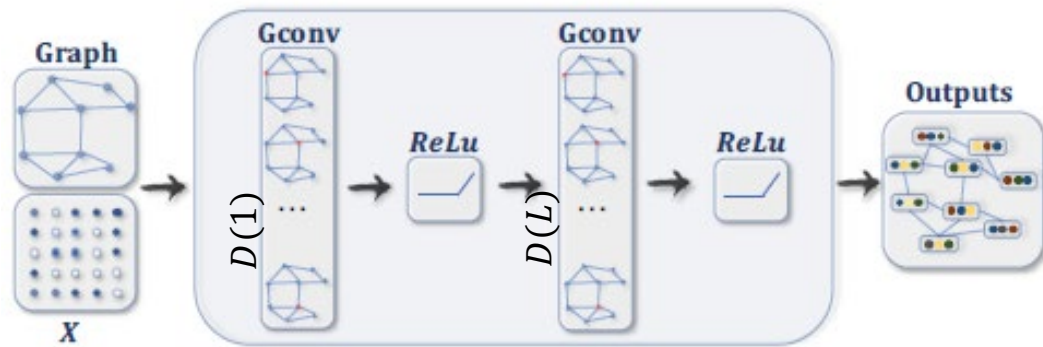
Node classification



Graph classification

Types of classification

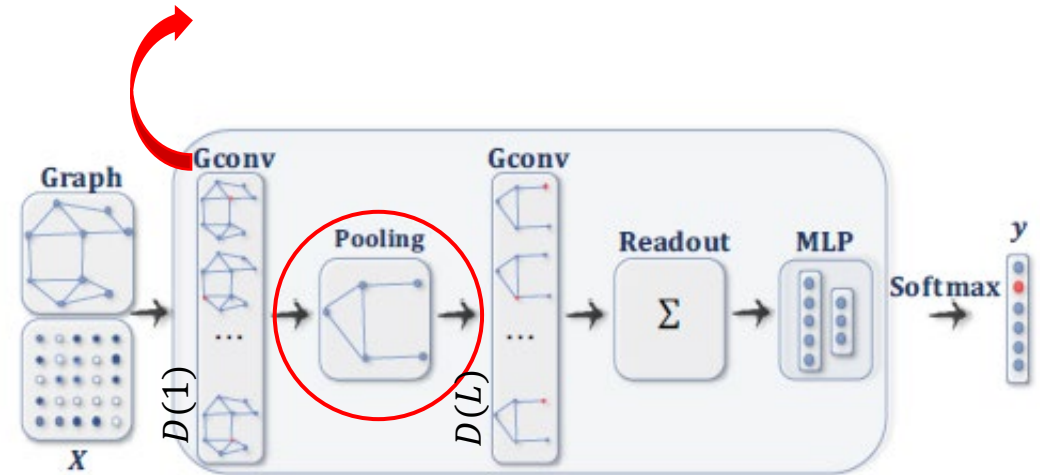
- **3 types:** edge, node, graph.



Node classification

$$X_{l+1} = \sigma(\hat{D}^{-\frac{1}{2}} \hat{A} \hat{D}^{-\frac{1}{2}} X_l W_l)$$

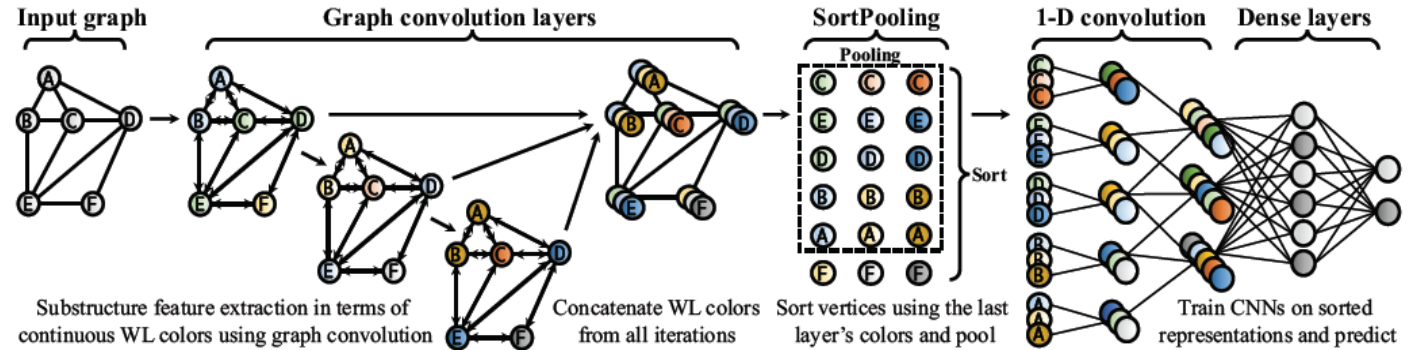
where $\hat{A} = (A + \mathbb{I})$, $\hat{D} = \sum_j \hat{A}_{i,j}$, σ is the activation function, and W_l is the trainable weight matrix.



Graph classification

Pooling layers

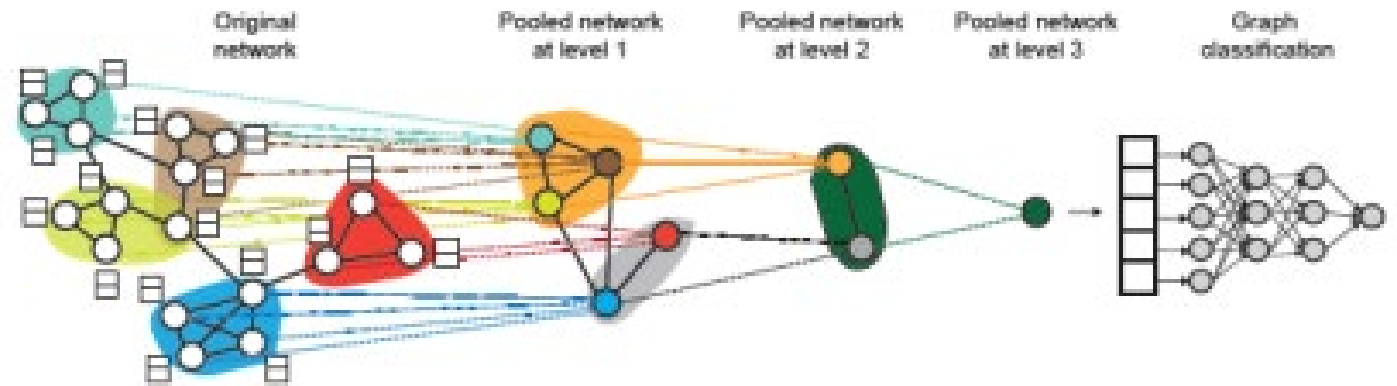
- SortPooling (DGCNN)



- DiffPool

$$H^{(l)} = S^{(l)T} H^{(l)}$$

where $S^{(l)} = \text{softmax}(GNN(A^{(l-1)}, H^{(l-1)}))$,
 $S^{(l)} \in \mathbb{R}^{n_{(l-1)} \times n_{(l)}}$,
 $H^{(l)} \in \mathbb{R}^{n_{(l)} \times d_{(l)}}$ and
 $H^{(l-1)} \in \mathbb{R}^{n_{(l-1)} \times d_{(l-1)}}$.



Bibliography

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